

## Chapter - 11

## STATISTICS

## Solutions

1. **(d):** Objectives of Constructing table for presenting data:
  1. To bring out the essential features of the data
  2. To facilitate statistical analysis
  3. Saving of Space
2. **(c):** Tabular presentation of data saves space without compromising "Quality of data" & "Quantity of data".
3. **(a):** When the quantitative and qualitative data are arranged according to a single feature, the tabulation is known as "One-way tabulation".
4. **(d):** The table where the variables are subdivided with interrelated features is known as two-way table.
5. **(c):** General tables of data used to show data in an orderly manner are called as repository tables.
6. **(a):** Required percentage =  $\frac{152.2}{86.4} \times 100 \approx 176\%$  approx.
7. **(b):** Clearly shown by table, oilseeds is the answer.
8. **(c):** Average production of pulses

$$= \frac{20.5+22.4+24.6+23.5+27.8+28.2}{6}$$

$$\Rightarrow \frac{147}{6} = 24.5 \text{ million tonnes.}$$

$$9. \text{ (a): Required percentage} = \frac{32.4}{450} \times 100 = 7.2\%$$

10. **(b):** Total production of oilseeds in the given years  
 $= 42.4 + 46.8 + 52.4 = 141.6$   
 Which is equal to the production of wheat in 1994-95

## Mean

$$11. \text{ (c): } \bar{x} = \frac{\sum x_i}{n}, \sum x_i = n\bar{x}$$

$$\text{New mean} = \frac{\sum \lambda x_i}{n} = \lambda \frac{\sum x_i}{n} = \lambda \bar{x}.$$

12. **(a):** It is obvious.

$$13. \text{ (b): } M_g = a + \frac{1}{\sum f_i} (\sum f_i d_i);$$

$$x = a \text{ i.e., } x = \text{assumed mean.}$$

14. **(c):** Let  $x_1, x_2, \dots, x_n$  be  $n$  observations.

$$\text{Then, } \bar{x} = \frac{1}{n} \sum x_i. \text{ Let } y_i = \frac{x_i}{\alpha} + 10$$

$$\text{Then, } \frac{1}{n} \sum_{i=1}^n y_i = \frac{1}{\alpha} \left( \frac{1}{n} \sum x_i \right) + \frac{1}{n} (10n)$$



$$\Rightarrow \bar{y} = \frac{1}{\alpha} \bar{x} + 10 = \frac{\bar{x} + 10\alpha}{\alpha}$$

15. (d): Since, root mean square  $\geq$  arithmetic mean

$$\therefore \sqrt{\frac{\sum_{i=1}^n x_i^2}{n}} \geq \frac{\sum_{i=1}^n x_i}{n} \Rightarrow \sqrt{\frac{400}{n}} \geq \frac{80}{n} \Rightarrow n \geq 16$$

Hence, possible value of  $n = 18$ .

16. (d): Required mean

$$\begin{aligned} &= \frac{(ax_1+b)+(ax_2+b)+\dots+(ax_n+b)}{n} \\ &= \frac{a(x_1+x_2+\dots+x_n)+nb}{n} = a\bar{x} + b. \\ &[\because \frac{x_1+x_2+\dots+x_n}{n} = \bar{x}] \end{aligned}$$

17. (a): It is obvious.

18. (c): It is a fundamental property.

19. (c): Total weight of 7 students is  $= 55 \times 7 = 385$  kg

Sum of weight of 6 students

$$= 52 + 58 + 55 + 53 + 56 + 54 = 328 \text{ kg}$$

$$\therefore \text{Weight of seventh student} = 385 - 328$$

$$= 57 \text{ kg.}$$

20. (b): Weighted mean  $= \frac{1.1^2 + 2.2^2 + \dots + n.n^2}{1^2 + 2^2 + \dots + n^2}$

$$= \frac{\sum n^3}{\sum n^2} = \frac{\frac{n(n+1)}{2} \cdot \frac{n(n+1)}{2}}{\frac{n(n+1)(2n+1)}{6}} = \frac{3n(n+1)}{2(2n+1)}$$

21. (d): Mean  $= \frac{1.1 + \frac{1}{2} \cdot 2 + \frac{1}{3} \cdot 3 + \frac{1}{4} \cdot 4 + \frac{1}{5} \cdot 5 + \dots + \frac{1}{n} \cdot n}{1+2+3+\dots+n}$

$$= \frac{1+1+1+\dots+1}{\frac{n(n+1)}{2}} = \frac{n}{\frac{n(n+1)}{2}} = \frac{2}{n+1}$$

22. (b):  $\frac{x_1+x_2+\dots+x_{10}}{10} = 4.5$

$$\Rightarrow x_1 + x_2 + \dots + x_{10} = 45$$

$$\text{And } \frac{x_{11}+x_{12}+\dots+x_{40}}{30} = 3.5$$

$$\Rightarrow x_{11} + x_{12} + \dots + x_{40} = 105$$

$$\therefore x_1 + x_2 + \dots + x_{40} = 150$$

$$\therefore \frac{x_1+x_2+\dots+x_{40}}{40} = \frac{150}{40} = \frac{15}{4}$$

23. (a): Marks obtained from 3 subjects out of 300  $=$

$$75 + 80 + 85 = 240$$

It the marks of another subjected is added, then the marks will be  $\leq 240$  out of 400

$$\therefore \text{Minimum average marks} = \frac{240}{4} = 60\%$$

[When marks in the fourth subject  $= 0$ ]

24. (b): A. M. = Sum of  $n$  terms.

Here the given sequence is in G. P.

$$\therefore a = 1, r = 3 > 1$$

$$\text{A. M.} = \frac{a(r^n-1)}{r-1} = \frac{1(3^n-1)}{3-1} = \frac{3^n-1}{2}$$

25. (c): Old avg. is  $x$

Then new avg. is  $(x + 2)$

According to question

$$15x + 70 = 16(x + 2)$$

$$15x + 70 = 16x + 32$$

$$x = 38$$

$$\text{New avg.} = 40.$$

26. (d):  $\frac{x_1+x_2+\dots+x_6}{16} = 16$

If  $x_1 = 16$

$$\frac{x_1+x_2+\dots+x_6-16+3+4+5}{18}$$

$$= \frac{16 \times 16 - 16 + 12}{18} = \frac{240 + 12}{18} = \frac{252}{18} = 14.$$

## Median and Mode

27. (d): It is obvious.

28. (b): It is obvious.

29. (c): It is a formula.

30. (d): It is a fundamental property.

31. (a): It is obvious.

32. (c): As the distribution is symmetrical, therefore,

$$Q_2(\text{Median}) = \frac{Q_1+Q_3}{2} = \frac{25+45}{2} = 35.$$

33. (d): Since,  $n = 6$ , then median term

$$= \left(\frac{n+1}{2}\right)^{\text{th}} = 5^{\text{th}} \text{ term.}$$

Now, last four observations are increased by 2.

$\therefore$  The median is 5<sup>th</sup> observation, which is remaining unchanged.

$\therefore$  There will be no change in median.

34. (c): It is obvious.

35. (d): It is obvious.

36. (a): Since  $x > 0$ ,

$\frac{x}{5}, \frac{x}{4}, \frac{x}{3}, \frac{x}{2}$ ,  $x$  is in ascending order.

$$\therefore \text{Median} = \frac{x}{3}$$

Also, median  $= 8$ . So,  $x = 24$

Relation between mean, median and mode, Pie diagram

37. (c): By the given condition,

$$\text{Mean} = (2 \text{ median})k \Rightarrow k = \frac{1}{2}$$

$$[\because \text{Mode} = 3 \text{ median} - 2 \text{ mean}]$$

38. (b): We know that,

$$\begin{aligned} \text{Mode} &= 3 \text{ Median} - 2 \text{ Mean} = 3(22) - 2(21) \\ &= 66 - 42 = 24. \end{aligned}$$

39. (d): It is a fundamental property.

40. (a): It is obvious.

41. (c): It is a fundamental property.

## Measures of dispersion

42. (d): It is obvious.

43. (b): It is a fundamental property.

44. (c): Median  $= 25.5a$

Mean deviation about median  $= 50$

$$\Rightarrow \frac{\sum |x_i - 25.5a|}{50} = 50$$

$$\Rightarrow 24.5a + 23.5a + \dots + 0.5a + 0.5a + \dots +$$

$$24.5a = 2500$$

$$\Rightarrow a + 3a + 5a + \dots + 49a = 2500$$

$$\Rightarrow \frac{25}{2}(50a) = 2500 \Rightarrow a = 4.$$



45. (c): Here,  $\bar{x} = \frac{2+4+6+8+10}{5} = 6$   
 Hence, variance =  $\frac{1}{n} \sum (x_i - \bar{x})^2$   
 $= \frac{1}{5} \{(2 - 6)^2 + (4 - 6)^2 + (6 - 6)^2 + (8 - 6)^2 + (10 - 6)^2\}$   
 $= \frac{1}{5} \{(16 + 4 + 0 + 4 + 16)\} = \frac{1}{5} \{40\} = 8.$

46. (c): It is obvious.  
 47. (a): It is obvious.  
 48. (d): It is obvious  
 49. (c): It is obvious.  
 50. (b): It is obvious.

51. (a): Variance = (S.D.)<sup>2</sup> =  $\frac{1}{n} \sum x^2 - \left(\frac{\sum x}{n}\right)^2$  [ $\because \bar{x} = \frac{\sum x}{n}$ ]  
 $= \frac{n(n+1)(2n+1)}{6n} - \left(\frac{n(n+1)}{2n}\right)^2 = \frac{n^2-1}{12}.$

52. (b): It is obvious.  
 53. (d): It is obvious.  
 54. (c): It is obvious.

55. (a): We know that, S.D. =  $\frac{3}{2}$  Q. D.  
 $\therefore$  S. D. =  $\frac{3}{2} \times 16 = 24.$

56. (a): We know that, Q.D. =  $\frac{5}{6} \times$  M. D. =  $\frac{5}{6} \times 12 = 10$   
 $\therefore$  S. D. =  $\frac{3}{2} \times$  Q. D. =  $\frac{3}{2} \times 10 \Rightarrow$  S. D. = 15.  
 Aliter : M. D. =  $\frac{4}{5}$  S. D.  $\Rightarrow 12 = \frac{4}{5}$  S. D.  
 $\therefore$  S. D. =  $\frac{12 \times 5}{4} = 15.$

57. (a): Data : 3, 4, 5, 7, 10, 10, 10  
 Median is 7 : Mean is also 7 [check :  $\frac{49}{7} = 7$ ] but mode is 10.  
 M.D. (from mode)  
 $= \frac{1}{7} (7 + 6 + 8 + 3 + 0 + 0 + 0) = \frac{1}{7} (21) = 3.$

58. (c):  
 59. (a, d):  $CV_1 = 60, CV_2 = 70, \sigma_1 = 21, \sigma_2 = 16$   
 Let  $\bar{x}_1, \bar{x}_2$  be the means of 1<sup>st</sup> and 2<sup>nd</sup> distribution respectively.  
 $\Rightarrow CV_1 = \frac{\sigma_1}{x_1} \times 100$   
 $\Rightarrow \bar{x}_1 = \frac{\sigma_1}{CV_1} \times 100 = \frac{21}{60} \times 100 = 35$   
 Similarly,  $\bar{x}_2 = \frac{\sigma_2}{CV_2} \times 100 = \frac{16}{70} \times 100 = 22.85.$

60. (a): Standard deviation of numbers 2, 3, a and 11 is 3.5  
 $\therefore (3.5)^2 = \frac{\sum x_i^2}{4} - (\bar{x})^2$   
 $\Rightarrow (3.5)^2 = \frac{4+9+a^2+121}{4} - \left(\frac{2+3+a+11}{4}\right)^2$   
 On solving, we get  
 $3a^2 - 32a + 84 = 0.$

61. (b): Given, observations are 3, 10, 10, 4, 7, 10 and 5.

$\therefore \bar{x} = \frac{3+10+10+4+7+10+5}{7} = \frac{49}{7} = 7$

$x_i$	$d_i =  x_i - \bar{x} $
3	4
10	3
10	3
4	3
7	0
10	3
5	2
Total	$\sum d_i = 18$

Now, M. D. =  $\frac{\sum d_i}{N} = \frac{18}{7} = 2.57$

62. (b): M.D. =  $\frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}|$

63. (a): Since, the lives of 5 bulbs are 1357, 1090, 1666, 1494 and 1623.

$\therefore$  Mean =  $\frac{1357+1090+1666+1494+1623}{5}$   
 $\Rightarrow \frac{7230}{5} = 1446$

$x_i$	$d_i =  x_i - \bar{x} $
1357	89
1090	356
1666	220
1494	48
1623	177
Total	$\sum d_i = 890$

M.D. =  $\frac{\sum d_i}{N} = \frac{890}{5} = 178.$

64. (c): Since, marks obtained by 9 students in Mathematics are 50, 69, 20, 33, 53, 39, 40, 65, 59  
 Rewrite the given data in ascending order  
 20, 33, 39, 40, 50, 53, 59, 65, 69

Here, n = 9 [odd]  
 $\therefore$  Median =  $\left(\frac{9+1}{2}\right)$  term = 5<sup>th</sup> term  
 Mean = 50

$x_i$	$d_i =  x_i - Me $
20	30
33	17
39	11
40	10
50	0
53	3
59	9
65	15
69	19
N = 9	$\sum d_i = 114$

$\therefore$  M. D. =  $\frac{114}{9} = 12.67.$



65. (a): Given, data are 6, 5, 9, 13, 12, 8, and 10.

$x_i$	$x_i^2$
6	36
5	25
9	81
13	169
12	144
8	64
10	100
$\sum x_i = 63$	$\sum x_i^2 = 619$

$$\begin{aligned} \therefore \text{S.D.} = \sigma &= \sqrt{\frac{\sum x_i^2}{N} - \left(\frac{\sum x_i}{N}\right)^2} = \sqrt{\frac{619}{7} - \left(\frac{63}{7}\right)^2} \\ &\Rightarrow \sqrt{\frac{7 \times 619 - 3969}{49}} \\ &\Rightarrow \sqrt{\frac{4333 - 3969}{49}} \\ &\Rightarrow \sqrt{\frac{364}{49}} = \sqrt{\frac{52}{7}} \end{aligned}$$

66. (c): S.D. is given by

$$\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$$

67. (c):  $\bar{x} = 50, n = 100$  and  $\sigma = 5$

$$\begin{aligned} \sum x_i^2 &=? \\ \therefore \bar{x} &= \frac{\sum x_i}{n} \\ \Rightarrow 50 &= \frac{\sum x_i}{100} \\ \therefore \sum x_i &= 50 \times 100 = 5000 \\ \text{Now, } \sigma &= \sqrt{\frac{\sum x_i^2}{n} - \left(\frac{\sum x_i}{n}\right)^2} \Rightarrow \sigma^2 = \frac{\sum x_i^2}{n} - (\bar{x})^2 \\ \Rightarrow 25 &= \frac{\sum x_i^2}{100} - (50)^2 \Rightarrow 25 = \frac{\sum x_i^2}{100} - 2500 \\ \Rightarrow 2525 &= \frac{\sum x_i^2}{100} \\ \therefore \sum x_i^2 &= 252500 \end{aligned}$$

68. (a): Given observations are a, b, c, d and e.

$$\begin{aligned} \text{Mean} = m &= \frac{a+b+c+d+e}{5} \\ \sum x_i &= a + b + c + d + e = 5m \\ \text{Now, mean} &= \frac{a+k+b+k+c+k+d+k+e+k}{5} \\ \Rightarrow \frac{(a+b+c+d+e)+5k}{5} &= m + k \\ \therefore \text{S.D.} &= \sqrt{\frac{\sum (x_i+k)^2}{n} - (m+k)^2} \\ &\Rightarrow \sqrt{\frac{\sum (x_i^2+k^2+2kx_i)}{n} - (m^2+k^2+2mk)} \\ &\Rightarrow \sqrt{\frac{\sum x_i^2}{n} - m^2 + \frac{2k\sum x_i}{n} - 2mk} \\ &\Rightarrow \sqrt{\frac{\sum x_i^2}{n} - m^2 + 2mk - 2mk} \quad \left[\because \frac{\sum x_i}{n} = m\right] \\ &\Rightarrow \sqrt{\frac{\sum x_i^2}{n} - m^2} \Rightarrow s \end{aligned}$$

$$\begin{aligned} 69. (c): \text{Here, } s &= \frac{\sum x_i}{5}, s = \sqrt{\frac{\sum x_i^2}{5} - \left(\frac{\sum x_i}{5}\right)^2} \\ \therefore \text{S.D.} &= \sqrt{\frac{k^2 \sum x_i^2}{5} - \left(\frac{k \sum x_i}{5}\right)^2} \\ &\Rightarrow \sqrt{\frac{k^2 \sum x_i^2}{5} - k^2 \left(\frac{\sum x_i}{5}\right)^2} = \sqrt{\left(\frac{\sum x_i^2}{5}\right) - \left(\frac{\sum x_i}{5}\right)^2} = ks \end{aligned}$$

70. (a):  $w_i = x_i + k, \bar{x}_i = 48, s_{x_i} = 12, w_i = 55$  and  $sw_i = 15$

$$\begin{aligned} \text{Then, } \bar{w}_i &= \bar{x}_i + k \\ [\text{where, } \bar{w}_i \text{ is mean } w_i\text{'s and } \bar{x}_i \text{ is mean of } x_i\text{'s}] \\ \Rightarrow 55 &= 48 + k \dots (i) \\ \text{Now, S.D. of } w_i &= \text{S.D. of } x_i \\ \Rightarrow 15 &= 12 \\ \Rightarrow 1 &= \frac{15}{12} \\ &= 1.25 \dots (ii) \\ \text{From Eqs. (i) and (ii),} \\ \Rightarrow k &= 55 - 1.25 \times 48 \\ &= -5 \end{aligned}$$

71. (d): We know that, S.D. of first n natural number

$$\begin{aligned} &= \sqrt{\frac{n^2-1}{12}} \\ \therefore \text{S.D. of first 10 natural numbers} &= \sqrt{\frac{(10)^2-1}{12}} \\ &= \sqrt{\frac{100-1}{12}} = \sqrt{\frac{99}{12}} = \sqrt{8.25} = 2.87 \end{aligned}$$

72. (d): Given numbers are 1, 2, 3, 4, 5, 6, 7, 8, 9, and 10.

$$\begin{aligned} \text{If 1 is added to each number, then observations} \\ \text{will be 2, 3, 4, 5, 6, 7, 8, 9, 10 and 11} \\ \therefore \sum x_i &= 2 + 3 + 4 + \dots + 11 \\ &= \frac{10}{2} [2 \times 2 + 9 \times 1] = 5[4 + 9] = 65 \\ \text{And } \sum x_i^2 &= 2^2 + 3^2 + 4^2 + 5^2 + \dots + 11^2 \\ &= (1^2 + 2^2 + 3^2 + \dots + 11^2) - (1^2) \\ &= \frac{11 \times 12 \times 23 - 6}{6} = 505 \\ \therefore s^2 &= \frac{\sum x_i^2}{n} - \left(\frac{\sum x_i}{n}\right)^2 = \frac{505}{10} - \left(\frac{65}{10}\right)^2 \\ \Rightarrow 50.5 &- (6.5)^2 \\ &= 50.5 - 42.25 \\ &= 8.25 \end{aligned}$$

73. (a): Since, the first 10 positive integers are 1, 2, 3, 4, 5, 6, 7, 8, 9 and 10.

$$\begin{aligned} \text{On multiplying each number by } -1 \text{ we get} \\ -1, -2, -3, -4, -5, -6, -7, -8, -9, -10. \\ \text{On adding 1 in each number, we get} \\ 0, -1, -2, -3, -4, -5, -6, -7, -8, -9 \\ \therefore \sum x_i &= 0 - 1 - 2 - 3 - 4 - 5 - 6 - 7 - 8 - 9 \\ &= -\frac{9 \times 10}{2} \\ &= -45 \\ \text{And } \sum x_i^2 &= 0^2 + (-1)^2 + (-2)^2 + \dots + (-9)^2 \\ &= \frac{9 \times 10 \times 19}{6} \\ &= 285 \end{aligned}$$

$$S. D. = \sqrt{\frac{285}{10} - \left(\frac{-45}{10}\right)^2} = \sqrt{\frac{285}{10} - \frac{2025}{100}}$$

$$\text{Now, variance} = (S. D.)^2 = (\sqrt{8.25})^2 = 8.25.$$

$$74. \text{ (d): Variance} = \frac{\sum x_i^2}{n} - \left(\frac{\sum x_i}{n}\right)^2$$

$$= \frac{18000}{60} - \left(\frac{960}{60}\right)^2 = 300 - 256 = 44.$$

$$75. \text{ (a): Here, } CV_1 = 50, CV_2 = 60, \bar{x}_1 = 30 \text{ and } \bar{x}_2 = 25$$

$$\therefore CV_1 = \frac{\sigma_1}{\bar{x}_1} \times 100 \Rightarrow 50 = \frac{\sigma_1}{30} \times 100$$

$$\therefore \sigma_1 = \frac{30 \times 50}{100} = 15 \text{ and } CV_2 = \frac{\sigma_2}{\bar{x}_2} \times 100$$

$$\Rightarrow 60 = \frac{\sigma_2}{25} \times 100$$

$$\therefore \sigma_2 = \frac{60 \times 25}{100} = 15$$

$$\text{Now, } \sigma_1 - \sigma_2 = 15 - 15 = 0.$$

$$76. \text{ (a): } \sigma_c = 5 \Rightarrow \frac{5}{9}(F - 32) = C$$

$$F = \frac{9C}{5} + 32$$

$$\sigma_F = \frac{9}{5} \sigma_C = \frac{9}{5} \times 5 = 9$$

Here,

$$\sigma_F^2 = (9)^2 = 81.$$

$$77. \text{ (d): Average production of sugar in years 1998, 1999, 2000 and 2001} = \frac{15+50+30+35}{4}$$

$$= 32.5 \text{ thousand metric tonnes}$$

And average production of sugar in years 2001, 2002, 2003, and 2004 =  $\frac{35+65+75+70}{4}$

$$= 61.25 \text{ thousand metric tonnes}$$

$$\therefore \text{Required difference} = 61.25 - 32.5 = 28.75$$

thousand metric tonnes

$$78. \text{ (a): In 1999, \% increase in production from the previous year} = \frac{50-15}{15} \times 100\% = 233.33\%$$

$$\text{In 2001, \% increase in production from the previous year} = \frac{35-30}{30} \times 100\% = 16.66\%$$

$$\text{In 2003, \% increase in production from the previous year} = \frac{75-65}{65} \times 100\% = 15.38\%$$

$$\therefore \text{In the remaining three was decrease.}$$

$$79. \text{ (d): In 1998 the value of sugar per thousand Metric tonne} = \frac{27.5}{15} = \text{Rs. 1.833 lakh}$$

$$\text{In 1999 the value of sugar per thousand Metric tonne} = \frac{80}{50} = \text{Rs. 1.600 lakh}$$

$$\text{In 2000 the value of sugar per thousand Metric tonne} = \frac{50}{30} = \text{Rs. 1.666 lakh}$$

$$\text{In 2001 the value of sugar per thousand Metric tonne} = \frac{57.5}{35} = \text{Rs. 1.642 lakh}$$

$$\text{In 2002 the value of sugar per thousand Metric tonne} = \frac{102.5}{65} = \text{Rs. 1.575 lakh}$$

$$\text{In 2003 the value of sugar per thousand Metric tonne} = \frac{117.5}{75} = \text{Rs. 1.571 lakh}$$

$\therefore$  It is the highest in the year = 1998.

$$80. \text{ (d): In 1998 the value of sugar per thousand Metric tonne} = \frac{27.5}{15} = \text{Rs. 1.833 lakh}$$

In 1999 the value of sugar per thousand Metric tonne =  $\frac{80}{50} = \text{Rs. 1.600 lakh}$

$$\text{In 2000 the value of sugar per thousand Metric tonne} = \frac{50}{30} = \text{Rs. 1.666 lakh}$$

In 2001 the value of sugar per thousand Metric tonne =  $\frac{57.5}{35} = \text{Rs. 1.642 lakh}$

$$\text{In 2002 the value of sugar per thousand Metric tonne} = \frac{102.5}{65} = \text{Rs. 1.575 lakh}$$

In 2003 the value of sugar per thousand Metric tonne =  $\frac{117.5}{75} = \text{Rs. 1.571 lakh}$

$$\text{It is the lowest in the year 2003.}$$

$$81. \text{ (a): Total production} = (15 + 50 + 30 + 35 + 65 + 75 + 70) \text{ thousand metric tonnes}$$

$$25\% \text{ of the total production} = \frac{25}{100} \times 340 = 85 \text{ thousand metric tonnes}$$

And the production of the year 1998 and 2004 =  $(15 + 70) = 85 \text{ thousand metric tonnes}$

$$82. \text{ (a): The frequency 25 corresponds to the class mark 800.}$$

$$\text{The common width of class intervals} = 400 - 200 = 200$$

$$\text{Therefore, Class interval} = \left\{ \left( 800 - \frac{200}{2} \right) - \left( 800 + \frac{200}{2} \right) \right\} = (700 - 900)$$

$$83. \text{ (b): The number of labourers has to fall in the class interval } 500 - 700 \text{ whose class mark is } 600. \text{ The frequency corresponding to the class mark } 600 \text{ is } 20.$$

Hence, the required number of labourers is 20.

$$84. \text{ (c): The largest number of labourers belong to the class interval whose class mark is } 400. \text{ The corresponding class interval is } \left( 400 - \frac{200}{2} \right) - \left( 400 + \frac{200}{2} \right), \text{ i.e. } (300 - 500).$$

So, the largest numbers of labourers have a weekly income of at least \$ 300 but less than \$ 500.

$$85. \text{ (a): Frequency of the class interval whose class mark is } 15 \text{ is } 18.$$

$$86. \text{ (b): A frequency polygon is obtained by connecting the mid-points of the tops of the rectangles in a histogram. Therefore, Statement b is correct.}$$

$$87. \text{ (b): Frequency of the class interval } 15 - 20 \text{ is } 25.$$

$$88. \text{ (b): Class interval having the greatest frequency (30) is } 20 - 25.$$

$$89. \text{ (b):}$$



Class Interval	Frequency	Cumulative Frequency
10 - 15	20	20
15 - 20	25	45
20 - 25	30	75
25 - 30	15	90
30 - 35	10	100
35 - 40	5	105

Cumulative frequency of the class interval 20 – 25 is 75.

**90. (c):**

Class Interval	Frequency	Cumulative Frequency
10 - 15	20	20
15 - 20	25	45
20 - 25	30	75
25 - 30	15	90
30 - 35	10	100
35 - 40	5	105

Cumulative frequency of the class interval 25 – 30 is 90.

**91. (d):**

Class Interval	Frequency	Cumulative Frequency
10 - 15	20	20
15 - 20	25	45
20 - 25	30	75
25 - 30	15	90
30 - 35	10	100
35 - 40	5	105

Cumulative frequency of the class interval 30 – 35 is 100.

**92. (a):** The class interval 10 – 20 has the greatest frequency as the rectangle corresponding to the interval has the greatest area, the height being the greatest.

**93. (c):** The class interval 30 – 40 has the least frequency as the rectangle corresponding to the interval has the least area, the height being the least.

**94. (d):** The class intervals (20 – 30) and (40 – 50) has the frequency of 40.

**95. (b):** The class intervals (30 – 40) has the frequency of 30.

**96. (c):**  $50 + 40 + 30 = 120$

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**CHASE**

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**ACADEMY**